

## COSC 341 – Tutorial 2

- Let  $A = \{a, b, c\}$  be a set.
  - Define a relation  $R$  on  $A$  that is irreflexive, asymmetric, and not transitive
  - Extend  $R$  to a relation  $R'$  that is reflexive
  - Extend  $R'$  to a relation  $R''$  that is symmetric
  - Extend  $R''$  to a relation  $R'''$  that is transitive
- Are the following relations reflexive, symmetric, transitive? If they are: How many equivalence classes do they have?
  - $\sim$  on  $\mathbb{N}$  with:  $a \sim b \iff a$  divides  $b$  ( $\frac{b}{a} \in \mathbb{N}$ )
  - $\sim$  on  $\mathcal{P}(\mathbb{N})$  with:  $A \sim B \iff A \cap B = \emptyset$
  - $\sim$  on  $\mathbb{N}$  with:  $a \sim b \iff a$  and  $b$  have the same last digit
- Show that the set of even natural numbers is countable.

## Homework

- Are the following relations reflexive, symmetric, transitive? If they are: How many equivalence classes do they have?
  - $\sim$  on  $\mathcal{P}(\mathbb{N})$  with:  $A \sim B \iff A \subseteq B$
  - $\sim$  on  $\mathbb{Z}$  with:  $a \sim b \iff a - b$  is a multiple of 8
  - $\sim$  on  $\mathcal{P}(\mathbb{N})$  with:  $A \sim B \iff A \cap B \neq \emptyset$
- Show that the set of even integers is countable.